Achievable

AP STATISTICS DUMP SHEET

Probability and sampling

Probability and random variables

- Basic probability rules:
  - $P(A^c) = 1 - P(A)$
  - $P(A \cup B) = P(A) + P(B) - P(A \cap B)$
  - $P(A \mid B) = \dfrac{P(A \cap B)}{P(B)}$
- Independence:
  - $P(A \mid B) = P(A)$
  - $P(A \cap B) = P(A)\,P(B)$
- Discrete random variable:
  - $\mu = \sum x_i p_i$
  - $\sigma^2 = \sum (x_i - \mu)^2 p_i = \sum x_i^2 p_i - \mu^2$
- Binomial distribution:
  - $P(X = k) = \binom{n}{k} p^k (1-p)^{n-k}$
  - $\mu = np$, $\sigma = \sqrt{np(1-p)}$
  - Conditions (BINS): binary outcomes, independent trials, a fixed number of trials, the same probability of success
- Geometric distribution:
  - $P(X = k) = (1-p)^{k-1} p$
  - $\mu = \dfrac{1}{p}$, $\sigma = \dfrac{\sqrt{1-p}}{p}$
- **Bayes' theorem:** $P(A \mid B) = \dfrac{P(B \mid A)\,P(A)}{P(B)}$
- Linear transformations:
  - $E(aX + b) = aE(X) + b$
  - $\mathrm{Var}(aX + b) = a^2 \,\mathrm{Var}(X)$

Sampling distributions

- **Central limit theorem:** for large n (typically $n \geq 30$), the sampling distribution of $\bar{x}$ is approximately normal whatever the population's shape, if the observations are independent
- **Unbiased estimator:** the mean of its sampling distribution equals the parameter
- **Sampling variability:** a statistic varies from sample to sample; $\hat{p}$ and $\bar{x}$ are unbiased estimators of p and μ
- **10% condition:** when sampling without replacement, keep n at no more than 10% of the population to treat observations as independent
- **Sampling distribution of a proportion:** $\hat{p} \sim N\left(p, \sqrt{\dfrac{p(1-p)}{n}}\right)$
- **Conditions:** $np \geq 10$ and $n(1-p) \geq 10$, with a random sample of no more than 10% of the population
- **Sampling distribution of a mean:** $\bar{x} \sim N\left(\mu, \dfrac{\sigma}{\sqrt{n}}\right)$